

INTRODUCTION TO COMPUTER SCIENCE

Dr. Yasmine El-Glaly

Fall 2013

Review

- Representing Info
- Integers:

Base 10 — $234 = 2 \cdot 10^2 + 3 \cdot 10^1 + 4 \cdot 10^0 = \sum_{i=0}^2 d_i \cdot 10^i$

Generally $d_{k-1} \dots d_1 d_0 = \sum_{i=0}^{k-1} d_i \cdot 10^i$.

Base 2 — $11101100 =$

$1 \cdot 2^7 + 1 \cdot 2^6 + 1 \cdot 2^5 + 0 \cdot 2^4 + 1 \cdot 2^3 + 1 \cdot 2^2 + 0 \cdot 2^1 + 0 \cdot 2^0 = \sum_{i=0}^7 b_i \cdot 2^i$

Generally $b_{k-1} \dots b_1 b_0 = \sum_{i=0}^{k-1} b_i \cdot 2^i$.

Storing Integers

Data Compression
Communication Errors

- The most popular system for representing integers within today's computers is **two's complement** notation
- Uses a fixed number of bits to represent each of the values in the system

Storing Integers

Data Compression
Communication Errors

a. Using patterns of length three

Bit pattern	Value represented
011	3
010	2
001	1
000	0
111	-1
110	-2
101	-3
100	-4

- Starting with a string of 0s and then counting in binary until the pattern consisting of a single 0 followed by 1s is reached
- Negative values are obtained by starting with a string of 1s and then counting backward in binary until the pattern consisting of a single 1 followed by 0s is reached

Storing Integers

Data Compression

Communication Errors

a. Using patterns of length three

Bit pattern	Value represented
011	3
010	2
001	1
000	0
111	-1
110	-2
101	-3
100	-4

b. Using patterns of length four

Bit pattern	Value represented
0111	7
0110	6
0101	5
0100	4
0011	3
0010	2
0001	1
0000	0
1111	-1
1110	-2
1101	-3
1100	-4
1011	-5
1010	-6
1001	-7
1000	-8

Storing Integers

Data Compression
Communication Errors

- In a two's complement system, the leftmost bit of a bit pattern indicates the sign of the value represented. Thus, the leftmost bit is often called the **sign bit**

a. Using patterns of length three

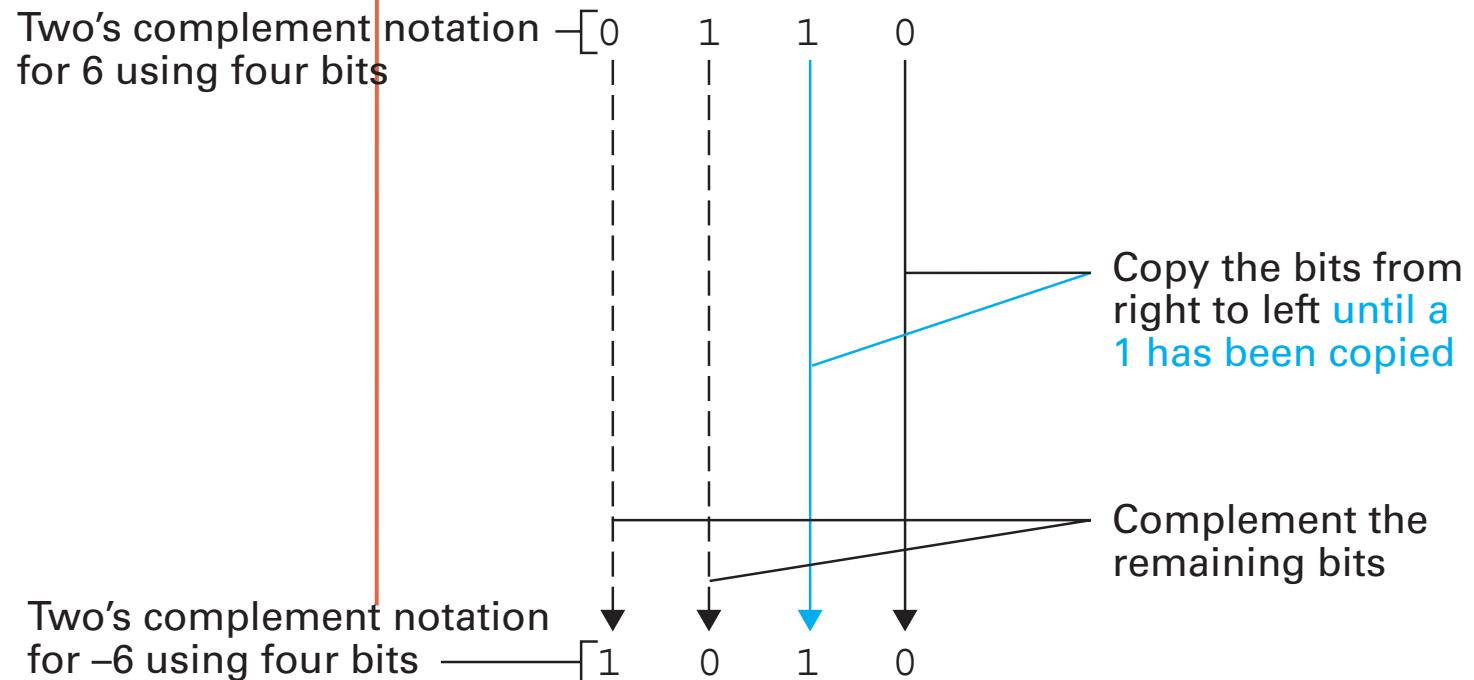
Bit pattern	Value represented
011	3
010	2
001	1
000	0
111	-1
110	-2
101	-3
100	-4

Storing Integers

Data Compression
Communication Errors

- An algorithm for converting back and forth between +ve and -ve values of the same magnitude

Figure 1.22 Encoding the value -6 in two's complement notation using 4 bits



Storing Integers

Data Compression
Communication Errors

- Addition in Two's Complement Notation
 - Same algorithm that we used for binary addition
 - Any extra bit generated on the left of the answer by a final carry must be truncated

Storing Integers

Data Compression
Communication Errors

- Example

**Problem in
base ten**

**Problem in
two's complement**

**Answer in
base ten**

$$\begin{array}{r} 3 \\ + 2 \\ \hline \end{array}$$



$$\begin{array}{r} 0011 \\ + 0010 \\ \hline 0101 \end{array}$$



5

$$\begin{array}{r} -3 \\ + -2 \\ \hline \end{array}$$



$$\begin{array}{r} 1101 \\ + 1110 \\ \hline 1011 \end{array}$$



-5

$$\begin{array}{r} 7 \\ + -5 \\ \hline \end{array}$$



$$\begin{array}{r} 0111 \\ + 1011 \\ \hline 0010 \end{array}$$



2

Storing Integers

Data Compression
Communication Errors

- Overflow problem
 - When using two's complement with patterns of 4 bits, the largest +ve integer that can be represented is 7, and the most -ve integer is -8
 - The value 9 can not be represented, which means that we cannot hope to obtain the correct answer to the problem $5 + 4$. In fact, the result would appear as -7
 - This phenomenon is called **overflow**

Storing Integers

Data Compression
Communication Errors

- Overflow problem
 - Today, it is common to use patterns of 32 bits for storing values in two's complement notation, allowing for positive values as large as 2,147,483,647 to accumulate before overflow occurs
 - The point is that computers can make mistakes. So, the person using the machine must be aware of the dangers involved

Storing Integers

Data Compression

Communication Errors

- Data Compression
 - For the purpose of storing or transferring data, it is often helpful (and sometimes mandatory) to reduce the size of the data
 - The technique for accomplishing this is called **data compression**

Storing Integers

Data Compression

Communication Errors

- Data compression
 - Generic Data Compression Techniques
- Compressing images
- Compressing audio and video

Storing Integers

Data Compression

Communication Errors

- Generic Data Compression Techniques
 - **Lossless** schemes
 - No loss in the info
 - **Lossy** schemes
 - May lead to the loss of info
 - Provides more compression

Storing Integers

Data Compression

Communication Errors

- **Run-length encoding**
 - Replace sequences of identical data elements with a code indicating the element that is repeated and the number of times it occurs in the sequence
 - For example, less space is required to indicate that a bit pattern consists of 253 ones, followed by 118 zeros, followed by 87 ones than to actually list all 458 bits.

Storing Integers

Data Compression

Communication Errors

- **Run-length encoding**
visualization



Storing Integers

Data Compression

Communication Errors

- **Differential Encoding**
 - Record the differences between consecutive data units rather than entire units
 - Each unit is encoded in terms of its relationship to the previous unit
 - Can be implemented in either lossless or lossy form
- Dictionary encoding: (can be lossy)
 - Lempel-Ziv methods: most popular for lossless — adaptive dictionary encoding
 - Lempel-Ziv-Welch (LZW): used a lot - GIF

Storing Integers

Data Compression

Communication Errors

- Images Compression
 - image consists of dots — pixels
 - 0—white; 1—black
 - colors — use more bits —
 - red, green, blue components
 - 3 bytes per pixel
 - example: 1024×1024 pixels
 - need to compress

Storing Integers

Data Compression

Communication Errors

- Images
 - GIF — Graphic Interchange Format
 - ◆ allows only 256 colors
 - PNG — Portable Network Graphic
 - JPEG — photographs
- Audio and Video
 - MPEG — Motion Picture Experts Group
 - MP3/MP4 most common for audio
- For audio/video — use properties of human hearing and sight

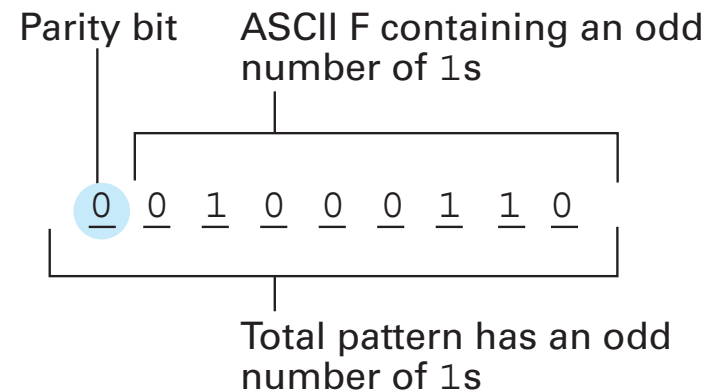
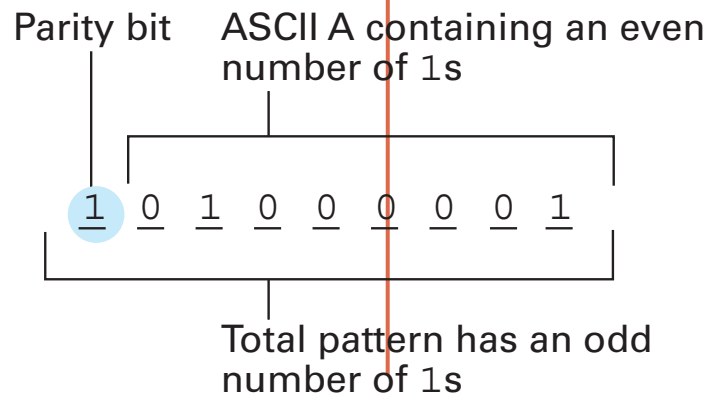
Storing Integers

Data Compression

Communication
Errors

- Reasons of data errors
 - Transferring
 - Malfunctioning circuit
 - Corrupt storage
- How to detect errors?
 - Parity bits
 - Odd, Even

Figure 1.28 The ASCII codes for the letters A and F adjusted for odd parity



Storing Integers

Data Compression

Communication
Errors

How to detect and even correct errors?

- Checksums (hashing or parity)
- Hamming distance – number of different bits
- 01010101 and 11010100
- Hamming distance 2

Assignment

- Read the rest of chapter 1
- Exercises:
 - 1
 - 7
 - 10
 - 12
 - 16
 - 24
 - 26
 - 32
 - 51

Thanks!

